

NEW CENTURY MATHS 11

MATHEMATICS STANDARD (PATHWAY 2)

FULLY WORKED SOLUTIONS

Chapter 2: Formulas and equations

SkillCheck

Question 1

a -27

b $9 - 3 = 6$

c -8

d $-5 \times (-5) = 25$

e -4

f $-2 + 4 = 2$

Question 2

a $8 \times 3 - 9 = 24 - 9$
 $= 15$

b $\frac{3+6}{3} = \frac{9}{3}$
 $= 3$

c $7 + 3 \times 3 = 7 + 9$
 $= 16$

d $\sqrt{12 \times 3} = \sqrt{36}$
 $= 6$

e $3^5 = 243$

f $2 \times 3^2 = 2 \times 9$
 $= 18$

Question 3

a $(-2)^2 - 4 = 4 - 4$
 $= 0$

b $3(-2+1) = 3 \times -1$
 $= -3$

c $8 - (-2) = 8 + 2$
 $= 10$

d $(-2)^7 = -128$

e $\frac{-18}{-2} = 9$

f $5 - 2 \times -2 = 5 + 4$
 $= 9$

Question 4

a $x - 3$

b $20 - a$

c -3

Question 5

a $3 \times 2x - 3 \times 1 = 6x - 3$

b $7 \times 4a + 7 \times 5 = 28a + 35$

c $-2 \times 6p - (-2) \times 2 = -12p + 4$

Question 6

a $3b = -15$

$$b = \frac{-15}{3}$$

$$b = -5$$

b $w - 8 = 9$

$$w = 9 + 8$$

$$w = 17$$

c $2r + 4 = 22$

$$2r = 22 - 4$$

$$2r = 18$$

$$r = \frac{18}{2}$$

$$r = 9$$

Question 7

$$A = \frac{1}{2}(10 + 15) \times 3$$

$$= \frac{1}{2} \times 25 \times 3$$

$$= 37.5$$

Exercise 2.01 Simplifying algebraic expressions

Question 1

a $2x^2 + x^2 + 3x + 2x = 3x^2 + 5x$

b $2ab + 5ab + a + b = 7ab + a + b$

c $-4m^2 + 6m^2 + 10 - 5 = 2m^2 + 5$

d $3r - 7r + 4ar - 2ar = -4r + 2ar$

e $y^2 + 2y - 5$

f $2a^2 - a^2 - 4 + 6 = a^2 + 2$

g $k^2 - 4k - 1$

h $-3de + 2d$

i $p^2 - p^2 - p - 5p = -6p$

j $7u - 3u - 5 - 10 = 4u - 15$

k $t^2 + t^2 + at + 2at = 2t^2 + 3at$

l $15x + 3x - 5 + 5 = 18x$

Question 2

a $4 \times 4 \times a \times a \times k \times m = 16a^2km$

b $-3 \times 8 \times c \times d \times d = -24cd^2$

c $\frac{1}{4} \times 10 \times t \times t^2 \times w \times w = \frac{10}{4}t^3w^2$
 $= \frac{5}{2}t^3w^2$

d $5 \times 5 \times x^3 \times x^3 = 25x^6$

e $9 \times \frac{2}{3} \times n^2 \times n^2 = \frac{18}{3} \times n^4$
 $= 6n^4$

f $7 \times 2 \times k^3 \times k^2 \times p \times p = 14k^5p^2$

g $-6 \times (-6) \times m \times n = 36mn$

h $5 \times \frac{3}{10} \times e \times e^2 = \frac{15}{10}e^3$
 $= \frac{3}{2}e^3$

i $2 \times 2 \times x \times x \times y^2 \times y^2 = 4x^2y^4$

j $10 \times (-2) \times a \times a \times b \times b = -20a^2b^2$

k $-4 \times \frac{1}{4} \times n^3 \times n^3 = -n^6$

l $-3 \times (-3) \times k \times k = 9k^2$

Question 3

a $\frac{4}{2} \times \frac{m}{m} = 2$

b $\frac{14}{2} \times \frac{x^2 y}{xy} = 7x$

c $\frac{-15}{3} \times \frac{e^2}{e^2} = -5$

d $\frac{10}{5} \times \frac{u^2 t^3}{ut^2} = 2ut$

e $3 \times \frac{x}{x^3} = 3 \times \frac{1}{x^2}$
 $= \frac{3}{x^2}$

f $\frac{27}{-9} \times \frac{pr}{pq} = \frac{-3r}{q}$

g $\frac{12}{20} \times \frac{g^2 h}{gh} = \frac{3}{5}g$ (OR $= \frac{3g}{5}$)

h $\frac{a^2}{a^3} = \frac{1}{a}$

i $\frac{15}{9} \times \frac{m^4 n}{m^2 n^2} = \frac{5}{3} \times \frac{m^2}{n}$
 $= \frac{5m^2}{3n}$

j $\frac{-4}{20} \times \frac{de}{e} = \frac{-1}{5} \times d$
 $= -\frac{d}{5}$

k $\frac{u}{4u} = \frac{1}{4}$

l $\frac{6}{24} \times \frac{wx^2}{w^2} = \frac{1}{4} \times \frac{x^2}{w}$
 $= \frac{x^2}{4w}$

Question 4

$$\frac{2}{5} \times \frac{-3}{10} \times \frac{xy}{y} = \frac{-6}{50} \times x$$
$$= -\frac{3x}{25}$$

$\therefore$ A

Question 5

a $\frac{45y^2}{4}$

b $\frac{8ah}{35}$

c $\frac{x^1}{y^1} \times \frac{y^2}{x^1} = 2$

d $\frac{20r}{6} \times \frac{1}{4r} = \frac{5}{6}$

e $\frac{4nw}{b} \times \frac{bn}{2w} = 2n^2$

f $\frac{3m}{6m} \times \frac{10n^2}{4n} = \frac{1}{2} \times \frac{5n}{2}$
 $= \frac{5n}{4}$

g $\frac{4a}{5} \times \frac{7}{2h} = \frac{14a}{5h}$

h $\frac{2e}{5} \times \frac{8}{3e} = \frac{16}{15}$
 $= 1\frac{1}{15}$

i $\frac{2de}{7p} \times \frac{14p}{4e} = d$

Question 6

a $-k^2 + 2k - 4k + 8 = -k^2 - 2k + 8$

b $\frac{1}{2} \times ay^2 \times y^2 = \frac{1}{2}ay^4$

c $\frac{-5t}{-20t} = \frac{1}{4}$

d $\frac{-32f^3g^2}{4f^2g} = -8fg$

e $-3c^2 - 7c^2 + 7c + 6c = -10c^2 + 13c$

f $-4z^2 + 4z + z + 8 = -4z^2 + 5z + 8$

g $-3 \times -2 \times a \times a^2 = 6a^3$

h $\frac{24cd}{8de} = \frac{3c}{e}$

i $2 - 4m^2 - 6m^2 - 2 = -10m^2$

j $\frac{20n^3x}{10nx^2} = \frac{2n^2}{x}$

k $4x^2 - 2xy + 4xy + 3x = 4x^2 + 2xy + 3x$

l $\frac{6a^4m^2}{-2a^2m^2} = -3a^2$

Exercise 2.02 Expanding algebraic expressions

Question 1

- a** $3 \times a + 3 \times 2 = 3a + 6$
- b** $5 \times 3 - 5 \times 2b = 15 - 10b$
- c** $-2 \times 2a + (-2) \times 1 = -4a - 2$
- d** $-6 \times b + -6 \times (-2) = -6b + 12$
- e** $3x \times x - 3x \times 2 = 3x^2 - 6x$
- f** $3p \times p - 3p \times a = 3p^2 - 3ap$
- g** $-4 \times 2k + (-4) \times 4 = -8k - 16$
- h** $2t \times 3 - 2t \times 4t = 6t - 8t^2$
- i** $-d \times d - (-d) \times 5 = -d^2 + 5d$
- j** $k \times 7 - k \times 5k = 7k - 5k^2$
- k** $-9b \times b - (-9)b \times 1 = -9b^2 + 9b$
- l** $2y \times 7x + 2y \times 4y = 14xy + 8y^2$

Question 2

- a** $-6n \times 4 - (-6n) \times n = -24n + 6n^2$
- b** $5x \times rx + 5x \times 2r = 5rx^2 + 10rx$
- c** $-1 \times 2a^2 - (-1) \times 4 = -2a^2 + 4$
- d** $5b \times a^2 + 5b \times 3b + 5b \times (-7) = 5a^2b + 15b^2 - 35b$
- e** $-1 \times x^2 - (-1) \times 4x + (-1) \times 10 = -x^2 + 4x - 10$
- f** $3h \times h - 3h \times 7e - 3h \times 4eh = 3h^2 - 21eh - 12eh^2$
- g** $y \times 2y + y \times 3 - y \times y^2 = 2y^2 + 3y - y^3$
- h** $de \times d^2 - de \times 2 + de \times e^2 = d^3e - 2de + de^3$
- i** $-3v \times (-3av) + (-3v) \times v - (-3v) \times 2a = 9av^2 - 3v^2 + 6av$

Question 3

a $5x + 20 - 2x - 6 = 3x + 14$

b $3d - 12 - 2d - 10 = d - 22$

c $6r + 60 - 4r + 20 = 2r + 80$

d $8f + 16 - f - 7 = 7f + 9$

e $6x - 12 - 15x - 20 = -9x - 32$

f $6x^2 + 24x - 3x^2 + 3x = 3x^2 + 27x$

g $3b^2 + 15b - b^2 + 8b = 2b^2 + 23b$

h $4w^2 - 28w - w^2 - w = 3w^2 - 29w$

i $6k + 6p + 3k + 6p = 9k + 12p$

j $2a - 2b + 2b + 2a = 4a$

k $2vx + 4x - vx - x = vx + 3x$

l $-3t - 3w - 4t + 2w = -7t - w$

m $3e^2 + 5e - 2e + e^2 = 4e^2 + 3e$

n $-2a - 6 + 4a - 12 = 2a - 18$

o $p^2 - pq - q^2 + pq = p^2 - q^2$

Question 4

a 2 and -2; opposites

b -6 and 6

c yes; $-b(b - a) = -b + a$

$$= a - b$$

Exercise 2.03 Formulas

Question 1

$$\begin{aligned}\mathbf{a} \quad 10^2 - (-3)^2 &= 100 - 9 \\ &= 91\end{aligned}$$

$$\begin{aligned}\mathbf{b} \quad \frac{10+6}{-3 \times 6} &= \frac{16}{-18} \\ &= -\frac{8}{9}\end{aligned}$$

$$\begin{aligned}\mathbf{c} \quad \sqrt{6+3 \times 10} &= \sqrt{36} \\ &= 6\end{aligned}$$

$$\begin{aligned}\mathbf{d} \quad 4[3 \times (-3) + 9] &= 4(-9 + 9) \\ &= 4 \times 0 \\ &= 0\end{aligned}$$

$$\begin{aligned}\mathbf{e} \quad 8 \times 6 + 4 \times (-3) &= 48 - 12 \\ &= 36\end{aligned}$$

$$\begin{aligned}\mathbf{f} \quad \frac{2 \times 10}{5} &= \frac{20}{5} \\ &= 4\end{aligned}$$

$$\begin{aligned}\mathbf{g} \quad 10(10 - 4) &= 10 \times 6 \\ &= 60\end{aligned}$$

$$\begin{aligned}\mathbf{h} \quad \sqrt{\frac{9 \times 10}{6+4}} &= \sqrt{\frac{90}{10}} \\ &= \sqrt{9} \\ &= 3\end{aligned}$$

$$\begin{aligned}\mathbf{i} \quad 6^2 + 6 &= 36 + 6 \\ &= 42\end{aligned}$$

$$\begin{aligned}\mathbf{j} \quad \frac{2 \times (-3) \times 6}{3} &= \frac{-36}{3} \\ &= -12\end{aligned}$$

$$\begin{aligned}\mathbf{k} \quad \sqrt{(-3)^2 + 7 \times 6 - 2} &= \sqrt{9 + 42 - 2} \\ &= \sqrt{49} \\ &= 7\end{aligned}$$

$$\begin{aligned}\mathbf{l} \quad (-3 - 10)^2 &= (-13)^2 \\ &= 169\end{aligned}$$

Question 2

$$\begin{aligned}V &= \pi \times 4.07^2 \times 11.58 \\ &= 602.625... \\ &\approx 602.63 \text{ cm}^3\end{aligned}$$

Question 3

$$\begin{aligned}\mathbf{a} \quad T &= 18 \times 4 + 28 \\ &= 100^\circ\text{C}\end{aligned}$$

$$\begin{aligned}\mathbf{b} \quad T &= 18 \times 1\frac{1}{2} + 28 \\ &= 55^\circ\text{C}\end{aligned}$$

$$\begin{aligned}\mathbf{c} \quad T &= 18 \times 0 + 28 \\ &= 28^\circ\text{C}\end{aligned}$$

Question 4

$$\begin{aligned}\mathbf{a} \quad US &= 0.722 \times 20 \\ &= \$14.44\end{aligned}$$

$$\begin{aligned}\mathbf{b} \quad US &= 0.722 \times 89.50 \\ &= \$64.619 \\ &\approx \$64.62\end{aligned}$$

$$\begin{aligned}\mathbf{c} \quad US &= 0.722 \times 4800 \\ &= \$3465.60\end{aligned}$$

Question 5

a v

b $v = 6 + 2 \times 5$
 $= 16 \text{ m/s}$

Question 6

a $m = 2 \times 8 + 1$
 $= 17$

b $m = 2 \times 40 + 1$
 $= 81$

c $m = 2 \times 150 + 1$
 $= 301$

Question 7

$$V = \frac{4}{3} \times \pi \times 14.5^3$$
$$= 12\,770.05\dots$$
$$\approx 12\,770.1 \text{ cm}^3$$

Question 8

$$T = 2\pi \sqrt{\frac{2.35}{10}}$$
$$= 2\pi \times \sqrt{0.235}$$
$$= 3.0458\dots$$
$$\approx 3.05 \text{ sec}$$

Question 9

$$A = 5600(1 + 0.094)^5$$
$$= \$8775.56$$

Question 10

$$d = \frac{11.5^2}{9.8}$$
$$= 13.494\dots$$
$$\approx 13.5 \text{ m}$$

Question 11

a B

c Increase her weight to around 65 kg.

b $B = \frac{60}{1.7^2}$
 $= 20.761\dots$
 ≈ 20.8

Question 12

$$\begin{aligned}\mathbf{a} \quad C &= \frac{5}{9}(77 - 32) \\ &= 25^{\circ}\text{C}\end{aligned}$$

$$\begin{aligned}\mathbf{c} \quad C &= \frac{5}{9}(59 - 32) \\ &= 15^{\circ}\text{C}\end{aligned}$$

$$\begin{aligned}\mathbf{b} \quad C &= \frac{5}{9}(100 - 32) \\ &= 37\frac{2}{9}^{\circ}\text{C} \\ &\approx 38^{\circ}\text{C}\end{aligned}$$

$$\begin{aligned}\mathbf{d} \quad C &= \frac{5}{9}(98.4 - 32) \\ &= 36.88...^{\circ}\text{C} \\ &\approx 37^{\circ}\text{C}\end{aligned}$$

Question 13

$$\begin{aligned}M &= \frac{5 \times 80}{18} \\ &= 22.22... \text{ m/s} \\ \therefore \mathbf{A}\end{aligned}$$

Question 14

$$\begin{aligned}\mathbf{a} \quad \text{Fried's rule} &= \frac{\text{age in months}}{150} \times \text{adult dosage} \\ &= \frac{24 \text{ months}}{150} \times 900 \\ &= 144 \text{ mg}\end{aligned}$$

$$\begin{aligned}\mathbf{b} \quad \text{Young's rule} &= \frac{\text{age in years}}{\text{age in years} + 12} \times \text{adult dosage} \\ &= \frac{2}{2 + 12} \times 900 \\ &= 128.57... \\ &\approx 129 \text{ mg}\end{aligned}$$

Question 15

$$\begin{aligned}\text{Clark's rule} &= \frac{\text{weight in kg}}{70} \times \text{adult dosage} \\ &= \frac{50 \text{ kg}}{70} \times 1680 \text{ mg} \\ &= 1200 \text{ mg}\end{aligned}$$

$\therefore \mathbf{A}$

Question 16

$$\text{Cowling's rule} = \frac{\text{age in years} + 1}{24} \times \text{adult dosage}$$

a $\frac{2 + 1}{24} \times 100 = 12.5 \text{ mg}$

b $\frac{6 + 1}{24} \times 100 = 29.16... \text{ mg} \approx 29.2 \text{ mg}$

c $\frac{10.5 + 1}{24} \times 100 = 47.916... \text{ mg} \approx 47.9 \text{ mg}$

Question 17

a Young's rule = $\frac{\text{age in years}}{\text{age in years} + 12} \times \text{adult dosage}$

$$\begin{aligned} &= \frac{1\frac{1}{2}}{1\frac{1}{2} + 12} \times 1000 \\ &= 111.11... \\ &\approx 111 \text{ mg} \end{aligned}$$

b Fried's rule = $\frac{\text{age in months}}{150} \times \text{adult dosage}$

$$\begin{aligned} &= \frac{18 \text{ months}}{150} \times 1000 \\ &= 120 \text{ mg} \end{aligned}$$

Question 18

$$\begin{aligned} d &= 8\sqrt{\frac{305}{5}} \\ &= 8 \times \sqrt{61} \\ &= 62.48... \\ &\approx 62 \text{ km} \end{aligned}$$

Question 19

$$\begin{aligned} P &= 450 + 0.11(2310 - 900) \\ &= 450 + 0.11 \times 1410 \\ &= \$605.10 \end{aligned}$$

Question 20

$$\begin{aligned}d &= \frac{6(6+1)}{2} \\&= \frac{6 \times 7}{2} \\&= \frac{42}{2} \\&= 21 \text{ m}\end{aligned}$$

Question 21

$$\begin{aligned}S &= 2\pi \times 3(3+8) \\&= 2 \times \pi \times 3 \times 11 \\&= 207.345... \\&= 207.35 \text{ cm}^2\end{aligned}$$

Question 22

$$\begin{aligned}V &= \sqrt{2 \times 9.8 \times 6\,378\,000} \\&= 11180.7333... \\&\therefore \text{B}\end{aligned}$$

Exercise 2.04 Solving equations

Question 1

a $3d + 2 = 20$
 $3d = 18$
 $d = 6$

b $2p - 3 = 2$
 $2p = 5$
 $p = \frac{5}{2}$
 $p = 2\frac{1}{2}$

c $4u + 6 = 20$
 $4u = 14$
 $u = 3\frac{1}{2}$

d $5a + 3 = -12$
 $5a = -15$
 $a = -3$

e $12b + 8 = 4$
 $12b = -4$
 $b = \frac{-4}{12}$
 $b = -\frac{1}{3}$

f $3 - 2a = -6$
 $-2a = -9$
 $a = \frac{-9}{-2}$
 $a = 4\frac{1}{2}$

g $3m = m - 10$
 $2m = -10$
 $m = -5$

h $\frac{3h}{4} = 9$
 $3h = 36$
 $h = 12$

i $\frac{r-1}{6} = 2$
 $r - 1 = 12$
 $r = 13$

j $\frac{-2x}{5} = 8$
 $-2x = 40$
 $x = -20$

k $\frac{y+2}{-3} = 1$
 $y + 2 = -3$
 $y = -5$

l $11 - 4n = 15$
 $-4n = 4$
 $n = \frac{4}{-4}$
 $n = -1$

m $5y + 6 = 4y + 11$
 $5y = 4y + 5$
 $y = 5$

n $\frac{4c}{10} = 3$
 $4c = 30$
 $c = \frac{30}{4}$
 $c = 7\frac{1}{2}$

o $\frac{z}{3} - 11 = 9$
 $\frac{z}{3} = 20$
 $z = 60$

Question 2

$$2t - 4 = 10 + t$$

$$2t = 14 + t$$

$$t = 14$$

$\therefore$ D

Question 3

a $5k - 13 = 3k + 9$

$$5k = 3k + 22$$

$$2k = 22$$

$$k = 11$$

b $8e = 2(e - 6)$

$$8e = 2e - 12$$

$$6e = -12$$

$$e = -2$$

c $\frac{2f + 7}{2} = 10$

$$2f + 7 = 20$$

$$2f = 13$$

$$f = 6\frac{1}{2}$$

d $3(x - 2) = 45$

$$3x - 6 = 45$$

$$3x = 51$$

$$x = 17$$

e $\frac{w}{5} - 8 = 6$

$$\frac{w}{5} = 14$$

$$w = 70$$

f $4(2d - 9) = -12$

$$8d - 36 = -12$$

$$8d = 24$$

$$d = 3$$

g $\frac{4n + 7}{9} = 2$

$$4n + 7 = 18$$

$$4n = 11$$

$$n = \frac{11}{4}$$

$$n = 2\frac{3}{4}$$

h $7u + 7 = 2u - 10$

$$7u = 2u - 17$$

$$5u = -17$$

$$u = \frac{-17}{5}$$

$$u = -3\frac{2}{5}$$

i $3p + 4 = 4p$

$$p = 4$$

j $\frac{5z + 8}{6} = -3$

$$5z + 8 = -18$$

$$5z = -26$$

$$z = \frac{-26}{5}$$

$$z = -5\frac{1}{5}$$

k $\frac{8 - 2b}{2} = 7$

$$8 - 2b = 14$$

$$-2b = 6$$

$$b = \frac{6}{-2}$$

$$b = -3$$

l $6(2 - 3q) = -24$

$$12 - 18q = -24$$

$$-18q = -36$$

$$q = \frac{-36}{-18}$$

$$q = 2$$

Question 4

$$\frac{c-4}{8} + 2 = 6$$

$$\frac{c-4}{8} = 4$$

∴ Line 2

(as says =8 but should be =4)

∴ A

Exercise 2.05 Formulas and equations

Question 1

a **i** $m = 3s + 1$
 $m = 3 \times 4 + 1$
 $m = 13$

ii $m = 3 \times 10 + 1$
 $m = 31$

b **i** $22 = 3s + 1$
 $21 = 3s$
 $s = 7$

ii $55 = 3s + 1$
 $54 = 3s$
 $s = 18$

Question 2

$$A = \frac{1}{2}bh$$

$$90 = \frac{1}{2} \times b \times 15$$

$$90 = 7\frac{1}{2}b$$

$$b = \frac{90}{7\frac{1}{2}}$$

$$b = 12 \text{ cm}$$

Question 3

a $s = \frac{d}{t}$
 $15 = \frac{d}{20}$
 $d = 15 \times 20$
 $d = 300 \text{ m}$

b $4.2 = \frac{250}{t}$
 $4.2t = 250$
 $t = \frac{250}{4.2}$
 $t = 59.523\dots$
 $t \approx 60 \text{ s}$

Question 4

$$A = \frac{1}{2}(x + y)h$$

$$22.5 = \frac{1}{2}(x + 7) \times 5$$

$$\frac{22.5}{5} = \frac{1}{2}(x + 7)$$

$$4.5 = \frac{1}{2}(x + 7)$$

$$9 = x + 7$$

$$x = 2 \text{ m}$$

Question 5

$$M = \frac{x + y + z}{3}$$

$$17 = \frac{x + 10 + 20}{3}$$

$$17 = \frac{x + 30}{3}$$

$$51 = x + 30$$

$$x = 21$$

Question 6

$$C = 2\pi r$$

$$50.27 = 2\pi r$$

$$r = \frac{50.27}{2\pi}$$

$$r = 8.0007...$$

$$r \approx 8 \text{ cm}$$

Question 7

$$A = P(1 + r)^n$$

$$6000 = P(1 + 0.11)^3$$

$$6000 = P \times 1.367631$$

$$P = \frac{6000}{1.367631}$$

$$P = 4387.148...$$

$$P \approx \$4387.15$$

Question 8

a $T = 18t + 28$

$$64 = 18t + 28$$

$$36 = 18t$$

$$t = 2 \text{ min}$$

b $92.8 = 18t + 28$

$$64.8 = 18t$$

$$t = \frac{64.8}{18}$$

$$t = 3.6 \text{ min}$$

Question 9

a $K = 1.61M$

$$5 = 1.61M$$

$$M = \frac{5}{1.61}$$

$$M = 3.105\dots$$

$$M = 3.11 \text{ miles}$$

b $1.5 = 1.61M$

$$M = \frac{1.5}{1.61}$$

$$M = 0.9316\dots$$

$$M = 0.93 \text{ miles}$$

Question 10

$$c = 2t + 2$$

a **i** $c = 2 \times 5 + 2$

$$c = 12$$

ii $c = 2 \times 12 + 2$

$$c = 26$$

b **i** $24 = 2t + 2$

$$22 = 2t$$

$$t = 11$$

ii $40 = 2t + 2$

$$38 = 2t$$

$$t = 19$$

Question 11

$$852 = 540 + 0.12(v - 2000)$$

$$312 = 0.12(v - 2000)$$

$$\frac{312}{0.12} = v - 2000$$

$$2600 = v - 2000$$

$$v = \$4600$$

Question 12

$$58 = 2 \times 4 \times 2 + 2 \times 4 \times h + 2 \times 2 \times h$$

$$58 = 16 + 8h + 4h$$

$$58 = 16 + 12h$$

$$42 = 12h$$

$$h = \frac{42}{12}$$

$$h = 3\frac{1}{2}$$

$$\therefore A$$

Question 13

$$12 = \frac{5k}{8}$$

$$96 = 5k$$

$$k = \frac{96}{5}$$

$$k = 19.2 \text{ km}$$

Question 14

$$m = 2t + 1$$

a $37 = 2t + 1$
 $36 = 2t$
 $t = 18$

b $55 = 2t + 1$
 $54 = 2t$
 $t = 27$

Question 15

$$46 = 18 + 14(h - 1)$$

$$28 = 14(h - 1)$$

$$2 = h - 1$$

$$h = 3 \text{ hours}$$

Question 16

$$F = 32 - 2t$$

a **i** $F = 32 - 2 \times 8$
 $F = 16 \text{ th}$

ii $F = 32 - 2 \times 14$
 $F = 4 \text{ th}$

b **i** $18 = 32 - 2t$
 $-14 = -2t$
 $t = \frac{-14}{-2}$
 $t = 7 \text{ seconds}$

ii $8 = 32 - 2t$
 $-24 = -2t$
 $t = \frac{-24}{-2}$
 $t = 12 \text{ seconds}$

Question 17

$$14\frac{1}{2} = 8 + \frac{18 - a}{2}$$

$$6\frac{1}{2} = \frac{18 - a}{2}$$

$$13 = 18 - a$$

$$-5 = -a$$

$$a = 5$$

$\therefore$ D

Question 18

$$44 = 8 + a \times 12$$

$$44 = 8 + 12a$$

$$36 = 12a$$

$$a = 3 \text{ m/s}^2$$

Exercise 2.06 Changing the subject of a formula

Question 1

a $y = 2x + 4$
 $2x + 4 = y$
 $2x = y - 4$
 $x = \frac{y - 4}{2}$

b $T = 3x - 7$
 $3x - 7 = T$
 $3x = T + 7$
 $x = \frac{T + 7}{3}$

c $d = \frac{x + 1}{3}$
 $\frac{x + 1}{3} = d$
 $x + 1 = 3d$
 $x = 3d - 1$

d $p = 18 - x$
 $18 - x = p$
 $-x = p - 18$
 $x = \frac{p - 18}{-1}$
 $x = -p + 18$
 $x = 18 - p$

e $k = 4x + r$
 $4x + r = k$
 $4x = k - r$
 $x = \frac{k - r}{4}$

f $C = n + \frac{x}{2}$
 $n + \frac{x}{2} = C$
 $\frac{x}{2} = C - n$
 $x = 2(C - n)$

g $S = 10bx$
 $10bx = S$
 $x = \frac{S}{10b}$

h $V = \frac{x - 5}{6}$
 $\frac{x - 5}{6} = V$
 $x - 5 = 6V$
 $x = 6V + 5$

i $z = 12 - ax$
 $12 - ax = z$
 $-ax = z - 12$
 $x = \frac{z - 12}{-a}$
 $x = \frac{12 - z}{a}$

Question 2

a $S = \frac{d}{t}$
 $\frac{d}{t} = S$
 $d = St$

b $S = \frac{d}{t}$
 $St = d$
 $t = \frac{d}{S}$

Question 3

a

$$\begin{aligned} A &= 180(n-2) \\ &= 180 \times (12-2) \\ &= 1800 \end{aligned}$$

$\therefore$ The angle sum is 1800° .

b

$$\begin{aligned} A &= 180(n-2) \\ 180(n-2) &= A \\ n-2 &= \frac{A}{180} \\ n &= \frac{A}{180} + 2 \end{aligned}$$

c

$$\begin{aligned} n &= \frac{A}{180} + 2 \\ &= \frac{1260^\circ}{180} + 2 \\ &= 9 \end{aligned}$$

$\therefore$ It has 9 sides.

Question 4

$$\begin{aligned} V &= \frac{1}{3}Ah \\ \frac{1}{3}Ah &= V \\ Ah &= 3V \\ A &= \frac{3V}{h} \end{aligned}$$

$\therefore$ D

Question 5

a

$$\begin{aligned} A &= \frac{1}{2}(a+b)h \\ \frac{1}{2}(a+b)h &= A \\ (a+b)h &= 2A \\ h &= \frac{2A}{a+b} \end{aligned}$$

b

$$\begin{aligned} A &= \frac{1}{2}(a+b)h \\ \frac{1}{2}(a+b)h &= A \\ (a+b)h &= 2A \\ a+b &= \frac{2A}{h} \\ b &= \frac{2A}{h} - a \end{aligned}$$

Question 6

a $A = \pi r^2$
 $\pi r^2 = A$
 $\pi = \frac{A}{r^2}$

b $y = mx + c$
 $mx + c = y$
 $mx = y - c$
 $m = \frac{y - c}{x}$

c $v^2 = u^2 + 2as$
 $u^2 + 2as = v^2$
 $2as = v^2 - u^2$
 $s = \frac{v^2 - u^2}{2a}$

d $z = \frac{x - m}{s}$
 $\frac{x - m}{s} = z$
 $x - m = sz$
 $x = sz + m$

e $E = mc^2$
 $mc^2 = E$
 $m = \frac{E}{c^2}$

f $K = \frac{1}{2}mv^2$
 $\frac{1}{2}mv^2 = K$
 $mv^2 = 2K$
 $m = \frac{2K}{v^2}$

g $A = P(1 + r)^n$
 $P(1 + r)^n = A$
 $P = \frac{A}{(1 + r)^n}$

h $x = 6y + 3$
 $6y + 3 = x$
 $6y = x - 3$
 $y = \frac{x - 3}{6}$

i $A = \frac{1}{2}bh$
 $\frac{1}{2}bh = A$
 $bh = 2A$
 $h = \frac{2A}{b}$

j $T^2 = \frac{4\pi^2 l}{g}$
 $\frac{4\pi^2 l}{g} = T^2$
 $4\pi^2 l = T^2 g$
 $l = \frac{T^2 g}{4\pi^2}$

k $V = IR - E$
 $IR - E = V$
 $IR = V + E$
 $R = \frac{V + E}{I}$

l $e = ir + \frac{Q}{C}$
 $ir + \frac{Q}{C} = e$
 $\frac{Q}{C} = e - ir$
 $Q = C(e - ir)$

m $s = ut + \frac{1}{2}at^2$
 $ut + \frac{1}{2}at^2 = s$
 $\frac{1}{2}at^2 = s - ut$
 $at^2 = 2(s - ut)$
 $a = \frac{2(s - ut)}{t^2}$

n $K = \frac{m + d}{w}$
 $\frac{m + d}{w} = K$
 $m + d = Kw$
 $d = Kw - m$

Question 7

Rearrange to get m as the subject:

$$B = \frac{m}{h^2}$$

$$\frac{m}{h^2} = B$$

$$m = Bh^2$$

If $B = 25$ and $h = 1.55$,

$$m = Bh^2$$

$$= 25 \times 1.55^2$$

$$= 60.0625$$

$$\approx 60$$

$\therefore$ The mass would be 60 kg.

Question 8

$$\text{If } V = \frac{1}{3}\pi r^2 h$$

$$\frac{1}{3}\pi r^2 h = V$$

$$\pi r^2 h = 3V$$

$$\therefore h = \frac{3V}{\pi r^2} \text{ as required.}$$

So, if $V = 3539.53 \text{ cm}^3$ and $r = 13 \text{ cm}$;

$$h = \frac{3V}{\pi r^2}$$

$$= \frac{3 \times 3539.53}{\pi \times 13^2}$$

$$= 20.000... \text{ cm}$$

$$= 20 \text{ cm}$$

$\therefore$ The height of the cone is 20 cm.

Question 9

$$C = \frac{5}{9}(F - 32)$$

$$\frac{5}{9}(F - 32) = C$$

$$F - 32 = \frac{9C}{5}$$

$$F = \frac{9C}{5} + 32$$

a If $C = 40$,

$$F = \frac{9C}{5} + 32$$

$$= \frac{9 \times 40}{5} + 32$$

$$= 104$$

b If $C = 100$,

$$F = \frac{9C}{5} + 32$$

$$= \frac{9 \times 100}{5} + 32$$

$$= 212$$

Question 10

$$M = \frac{10}{\pi h P}$$

$$\pi h P M = 10$$

$$\therefore P = \frac{10}{\pi h M}$$

If $M = 9.8$ and $h = 0.27$,

$$P = \frac{10}{\pi h M}$$

$$= \frac{10}{\pi \times 0.27 \times 9.8}$$

$$= 1.202...$$

$$\approx 1.2$$

Sample HSC problem

a
$$\begin{aligned} C &= 60 + 32(h - 1) \\ &= 60 + 32(2\frac{1}{2} - 1) \\ &= 60 + 32 \times 1\frac{1}{2} \\ &= \$108 \end{aligned}$$

b
$$\begin{aligned} C &= 60 + 32h - 32 \\ &= 28 + 32h \\ C - 28 &= 32h \\ h &= \frac{C - 28}{32} \end{aligned}$$

c
$$\begin{aligned} 172 &= 60 + 32(h - 1) \\ 112 &= 32(h - 1) \\ \frac{112}{32} &= h - 1 \\ h - 1 &= 3\frac{1}{2} \\ h &= 4\frac{1}{2} \text{ hours} \end{aligned}$$

Test yourself 2

Question 1

a $2t^2 - t^2 + 5ut + 4ut = t^2 + 9ut$

b $3 \times 5 \times k^2 \times k = 15k^3$

c $\frac{-9 \times 2}{3} \times d \times d = -6d^2$

d $8 \times 4 \times p^2 \times p^3 = 32p^5$

e $4h - 10h - 1 + 8 = -6h + 7$

f $8r^2$

g $-3d^2 \times (-3d^2) \times (-3d^2) = -27d^6$

h $\frac{3}{5}$

i $\frac{-3}{21} \times \frac{v^2 w^2}{vw} = -\frac{vw}{7}$

j $10x^2 - 2x^2 + 7x + x = 8x^2 + 8x$

k $\frac{3c}{b}$

l $-\frac{1}{a^2}$

m $\frac{48r}{6} \times \frac{1}{4r} = 8r \times \frac{1}{4r} = 2$

n $\frac{2y}{3} \times \frac{v}{1} = \frac{2vy}{3}$

o $\frac{x}{6} \times \frac{1}{2} = \frac{x}{12}$

p $\frac{3y}{2a} \times \frac{10d}{9dy} = \frac{1}{a} \times \frac{5}{3}$
 $= \frac{5}{3a}$

Question 2

- a** $5 \times 2x - 5 \times 4 = 10x - 20$
- b** $-3 \times a + (-3) \times 7 = -3a - 21$
- c** $4 \times 12t - 4 \times y = 48t - 4y$
- d** $-9 \times r^2 + (-9) \times 2w = -9r^2 - 18w$
- e** $8mn \times m - 8mn \times n = 8m^2n - 8mn^2$
- f** $-2d \times 4d - (-2d) \times d^2 = -8d^2 + 2d^3$

Question 3

- a** $12x + 3 + 2x - 4 = 14x - 1$
- b** $2n^2 - 2n + n - 1 = 2n^2 - n - 1$
- c** $12 - 6d - 4d + 12 = 24 - 10d$
- d** $p^2 + 4p - p^2 - 8p = -4p$
- e** $12u + 15 - u - 7 = 11u + 8$
- f** $5h^2 - h + 3h^2 + 27h = 8h^2 + 26h$

Question 4

- a** $3 \times 4^2 + 4 \times 20 = 48 + 80$
 $= 128$
- b** $\frac{7 \times 20}{-5} = \frac{140}{-5}$
 $= -28$
- c** $4 \times (-5) \times 20 = -400$
- d** $\sqrt{4(20 - (-5))} = \sqrt{4 \times 25}$
 $= \sqrt{100}$
 $= 10$

Question 5

$$\begin{aligned} S &= \pi \times 5(5 + 8) \\ &= \pi \times 5 \times 13 \\ &= 204.203... \\ &\approx 204.20 \text{ cm}^2 \end{aligned}$$

Question 6

$$\begin{aligned}P &= 480 + \frac{3400 - 1200}{10} \\&= 480 + \frac{2200}{10} \\&= 480 + 220 \\&= \$700\end{aligned}$$

Question 7

a $5p - 4 = 21$
 $5p = 25$
 $p = 5$

b $-2a + 6 = 8$
 $-2a = 2$
 $a = \frac{2}{-2}$
 $a = -1$

c $\frac{b-3}{2} = -6$
 $b - 3 = -12$
 $b = -9$

d $23 - 8r = 19$
 $-8r = -4$
 $r = \frac{-4}{-8}$
 $r = \frac{1}{2}$

e $\frac{4n}{5} = 11$
 $4n = 55$
 $n = \frac{55}{4}$
 $n = 13\frac{3}{4}$

f $\frac{r}{3} + 7 = 1$
 $\frac{r}{3} = -6$
 $r = -18$

g $\frac{20 - 4n}{4} = 7$
 $20 - 4n = 28$
 $-4n = 8$
 $n = \frac{8}{-4}$
 $n = -2$

h $3t + 13 = t - 12$
 $3t = t - 25$
 $2t = -25$
 $t = -12\frac{1}{2}$

i $5(2g - 4) = -30$
 $10g - 20 = -30$
 $10g = -10$
 $g = -1$

Question 8

$$28^2 = 11^2 + 2 \times 3 \times s$$

$$784 = 121 + 6s$$

$$663 = 6s$$

$$s = 110.5 \text{ m}$$

Question 9

$$13 = \frac{c}{8} + 3$$

$$10 = \frac{c}{8}$$

$$c = 80$$

Question 10

$$P = 110 + \frac{y}{2}$$

$$P - 110 = \frac{y}{2}$$

$$y = 2P - 220$$

$$y = 124 \times 2 - 220$$

$$y = 28 \text{ years}$$